
GPU-Accelerated Join Selectivity Estimation using KDE Models

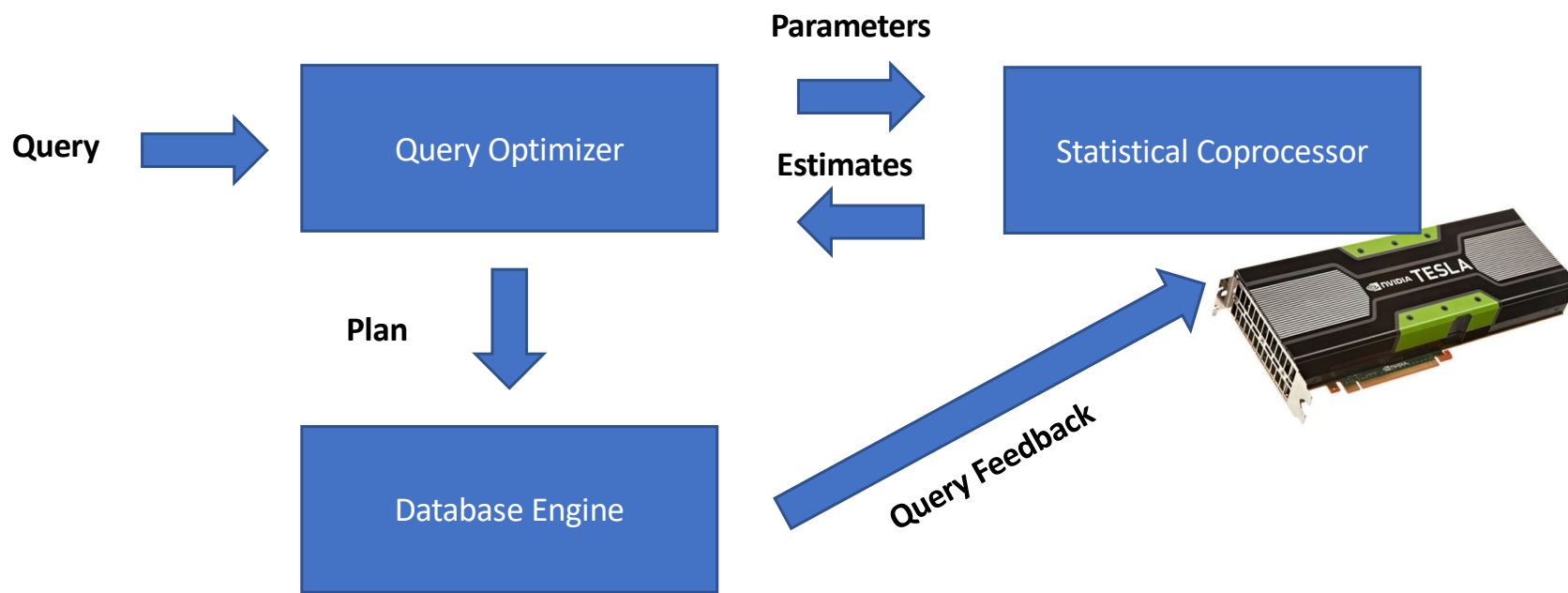
Paper:

Estimating Join Selectivities using Bandwidth-Optimized Kernel Density Models,

Martin Kiefer, Max Heimes, Sebastian Breß, Volker Markl

PVLDB, Volume 10 Issue 13, September 2017

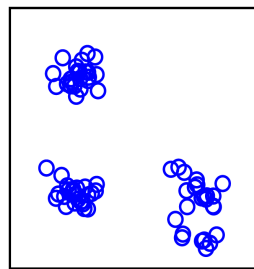
GPU-Accelerated Kernel Density Estimation for Join Selectivity Estimation



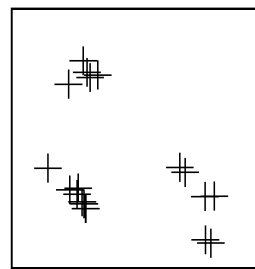
Background: Kernel Density Estimators

Average... ... over the kernel contributions

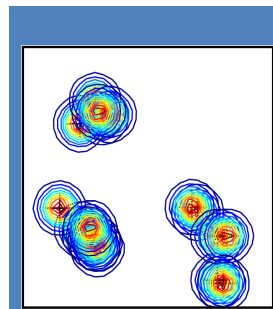
$$\hat{P}_H(\vec{x}) = \frac{1}{|S|} \sum_{i=1}^{|S|} K_H(s_i, \vec{x})$$



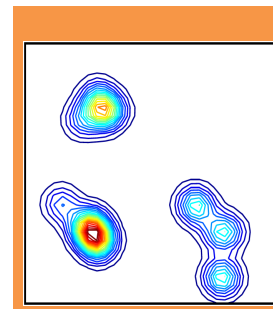
Dataset



Sample S



Kernels K_H

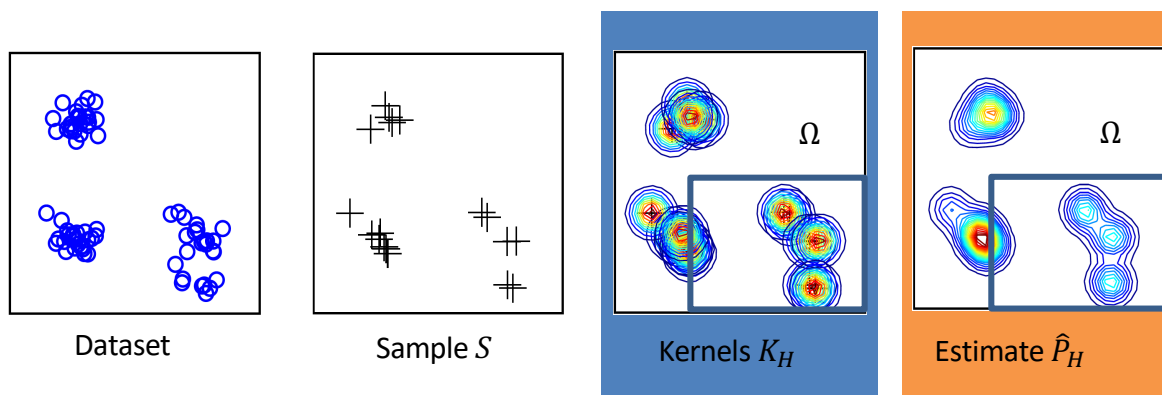


Estimate \hat{P}_H

Background: Kernel Density Estimators

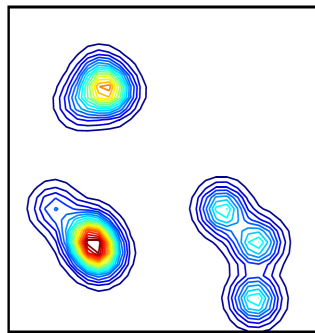
Average... ... over the kernel contributions

$$\text{sel}(\Omega) = \frac{1}{|S|} \sum_{i=1}^{|S|} \int_{\Omega} K_H(s_i, \vec{x}) d\vec{x}$$

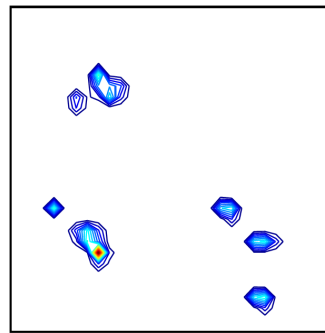


Background: Kernel Density Estimators for Multi-Dimensional Selectivity Estimation [1]

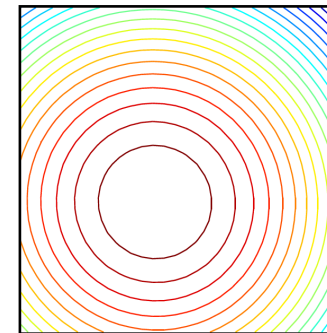
The bandwidth matrix H controls the smoothing applied on the sample



Good fit



Overfit



Underfit

- Range selections over base tables
- Bandwidth optimization based on the estimation error
- Easy model maintenance

The Problem: Multi-Dimensional Join Selectivity Estimation

$$Q = \sigma_{c_1} (R_1) \bowtie_{R_1.A_1=R_2.A_1} \sigma_{c_2} (R_2)$$

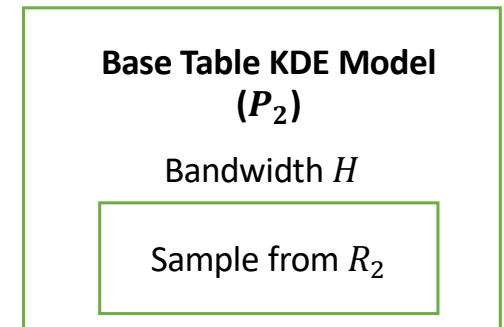
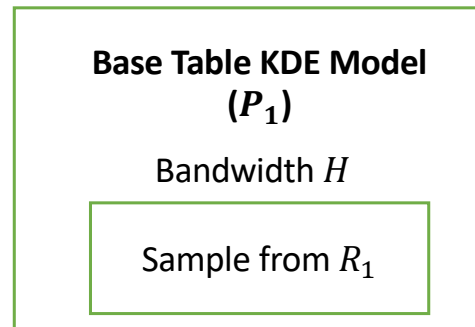
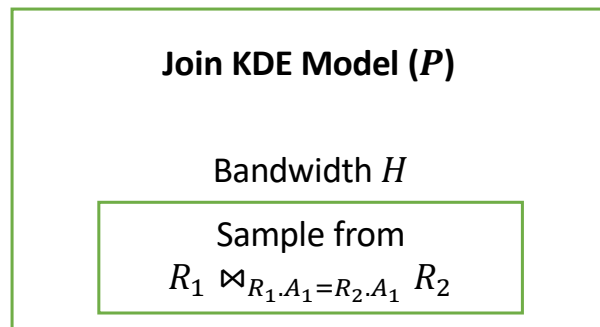
- and generalization to multiple joins
- **Databases:** Independence Assumption
 - Often violated
 - Introduce large errors, potentially bad query plans
- **Research:** Various Methods (e.g. Sampling, Sketches)
- **Our Approach:** Kernel Density Estimators

Why KDEs for Join Selectivities?

- Multivariate Estimator
- No independence assumption
- Hybrid between samples and histograms
 - Small bandwidth: Sample evaluation
 - Increasing bandwidth: More smoothing, increasing bucket sizes
 - Bandwidth optimization selects proper bandwidth

The Approach: Join and Base Table Models

$$Q = \sigma_{c_1} (R_1) \bowtie_{R_1.A_1=R_2.A_1} \sigma_{c_2} (R_2)$$



Compute: $P(c_1 \wedge c_2)$

Compute: $\sum_{v \in A} P_1(A_1 = v \wedge c_1) \cdot P_2(A_2 = v \wedge c_2)$



Easy to evaluate, better estimates



Support for base table and join selectivities
 Easy to construct and to maintain

Table Model: Computation Components

$$Q = \sigma_{c_1} (R_1) \bowtie_{R_1.A_1=R_2.A_1} \sigma_{c_2} (R_2)$$

Selectivity:

$$\frac{1}{s_1 \cdot s_2} \sum_{i=1, j=1}^{s_1, s_2} \hat{p}_1^{(i)}(c_1) \cdot \hat{p}_2^{(j)}(c_2) \cdot \hat{J}_{i,j}$$

The diagram shows the formula with three colored brackets underneath it. An orange bracket is under the denominator $s_1 \cdot s_2$. A green bracket is under the product of the two probability terms $\hat{p}_1^{(i)}(c_1) \cdot \hat{p}_2^{(j)}(c_2)$. A blue bracket is under the distance function term $\hat{J}_{i,j}$.

Sum over cross
product of two
samples

Invariant Contributions:
Contribution of sample
points wrt. selection
predicate

Cross Contribution:
Distance function on join
attributes of sample points

Table Model: Sample Pruning

$$\frac{1}{s_1 \cdot s_2} \sum_{i=1, j=1}^{s_1, s_2} \hat{p}_1^{(i)}(c_1) \cdot \hat{p}_2^{(j)}(c_2) \cdot \hat{J}_{i,j}$$

Sample 1

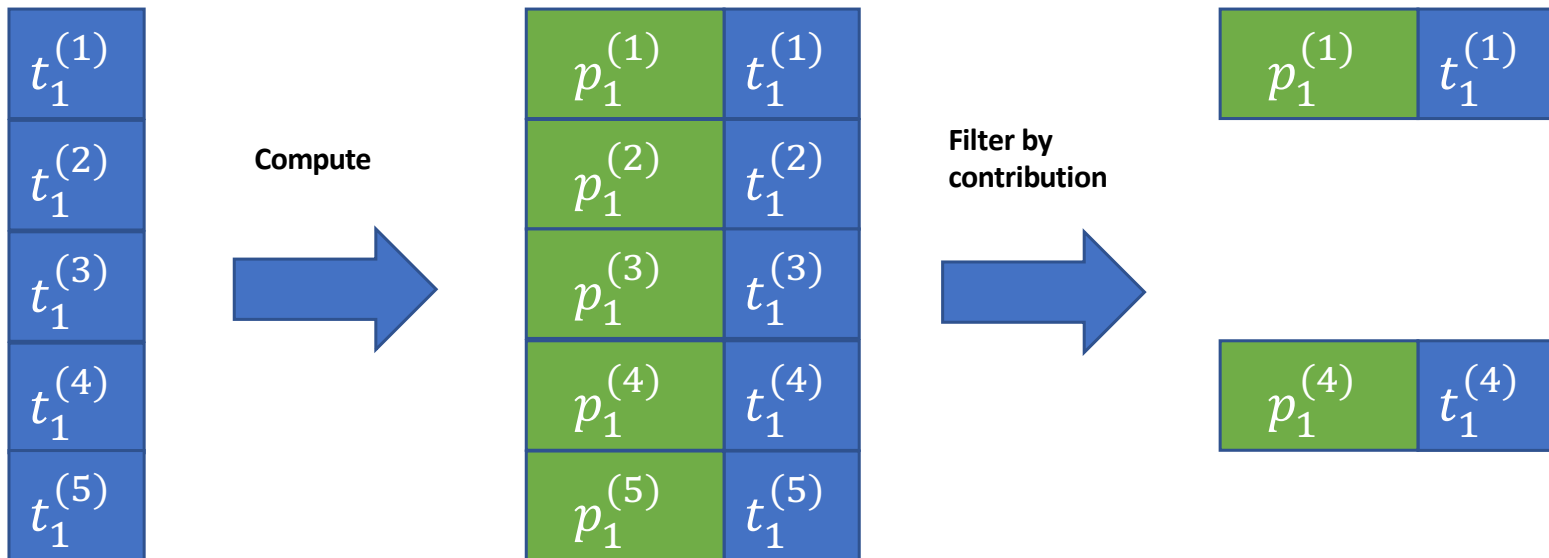
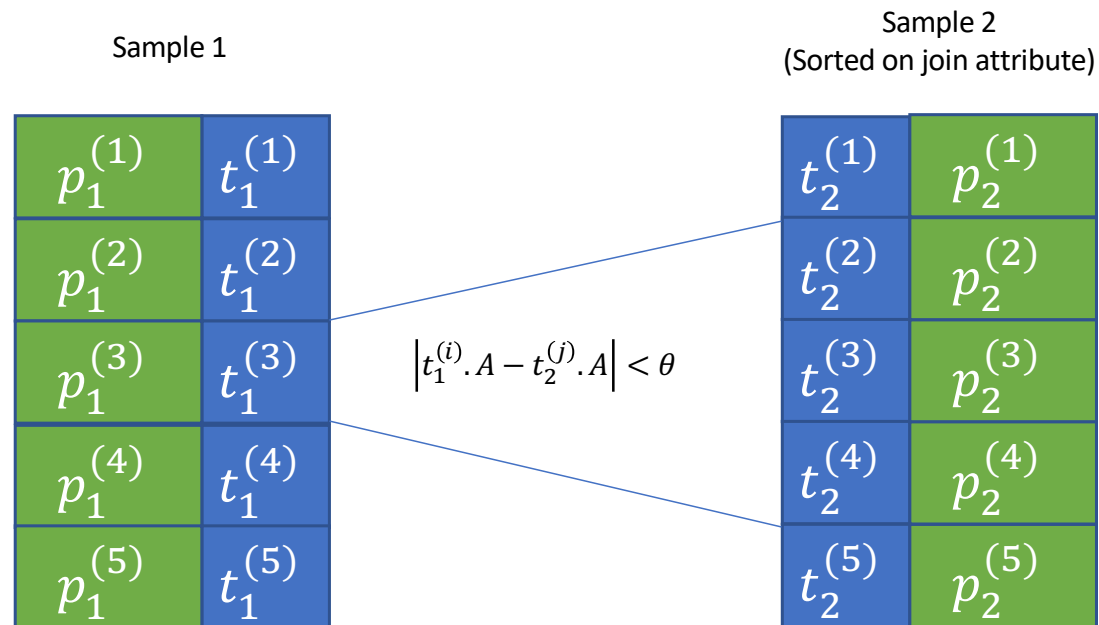


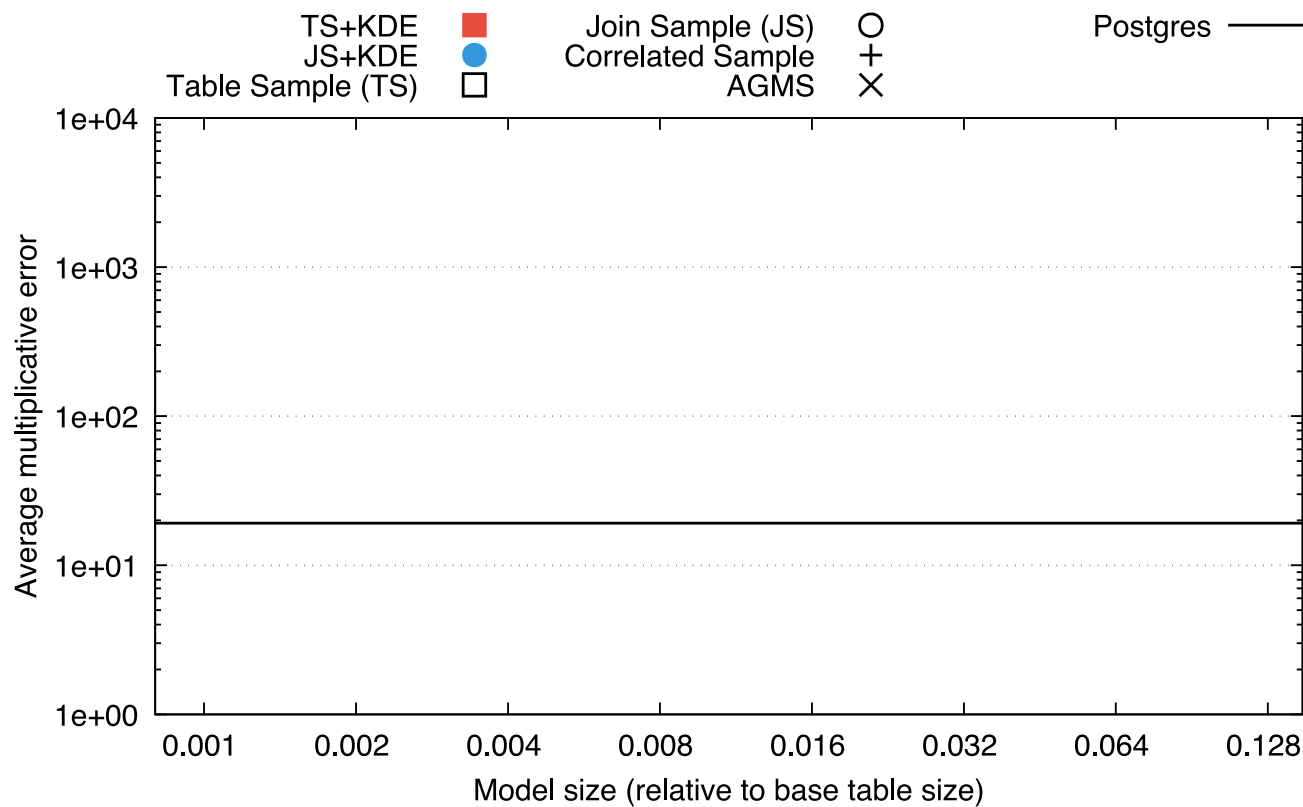
Table Model: Cross Pruning

$$\frac{1}{s_1 \cdot s_2} \sum_{i=1, j=1}^{s_1, s_2} \hat{p}_1^{(i)}(c_1) \cdot \hat{p}_2^{(j)}(c_2) \cdot \hat{J}_{i,j}$$



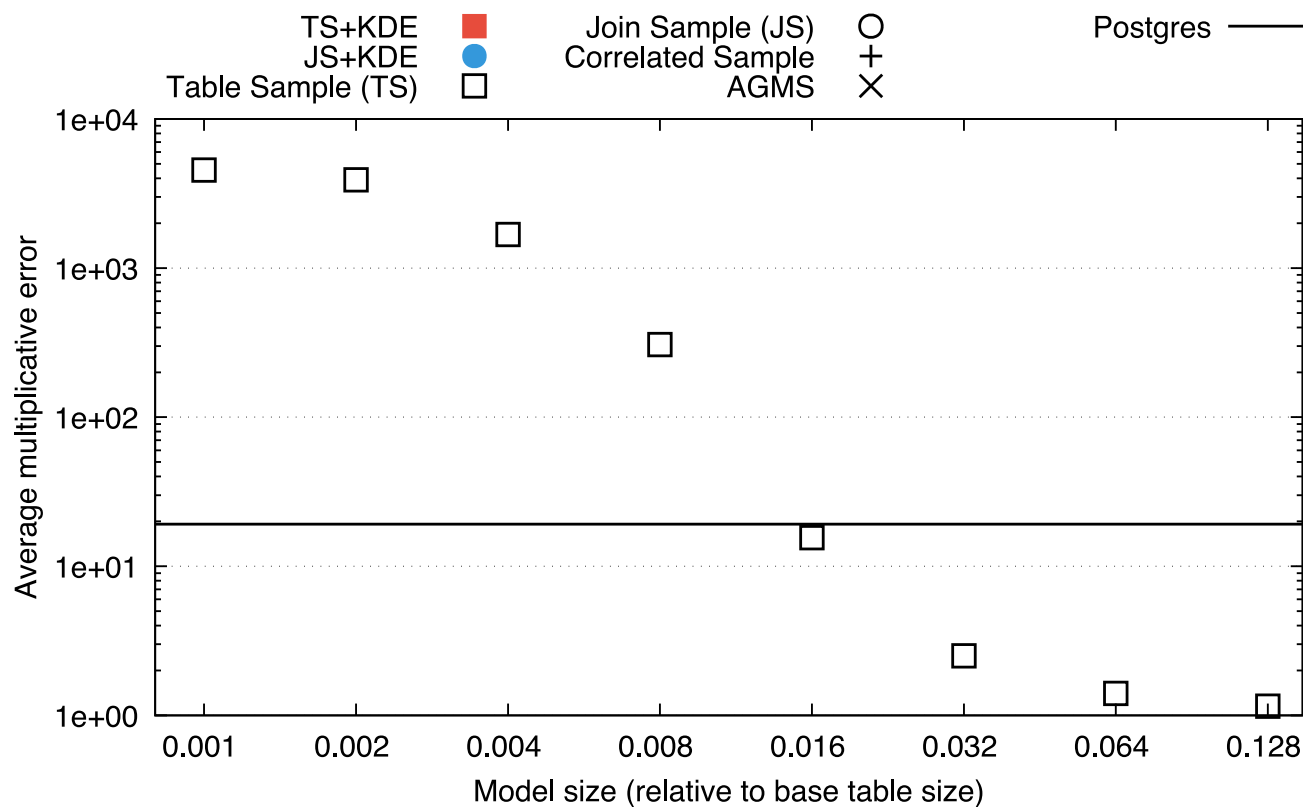
Evaluation: Scaling the Model Size (Postgres)

Dataset: DMV
Query: Q1U



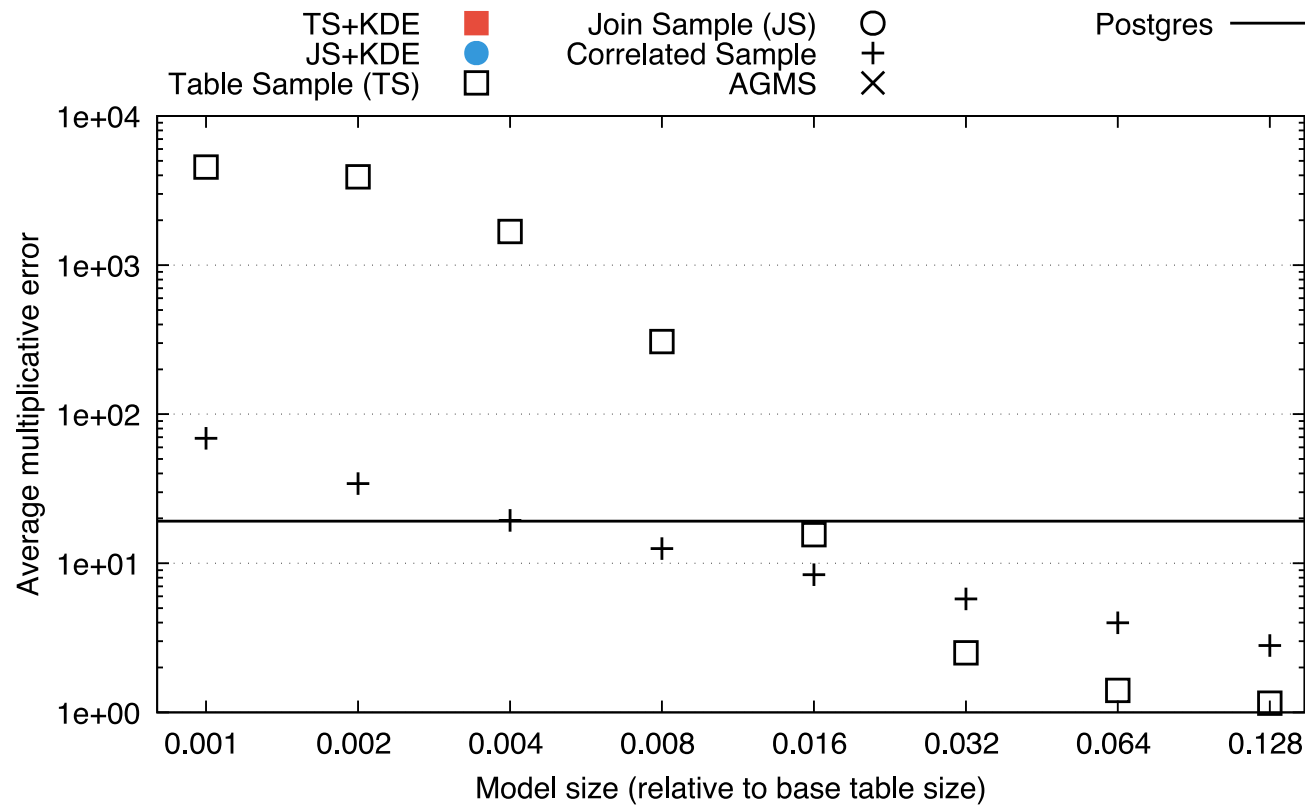
Evaluation: Scaling the Model Size (Table Sample)

Dataset: DMV
Query: Q1U



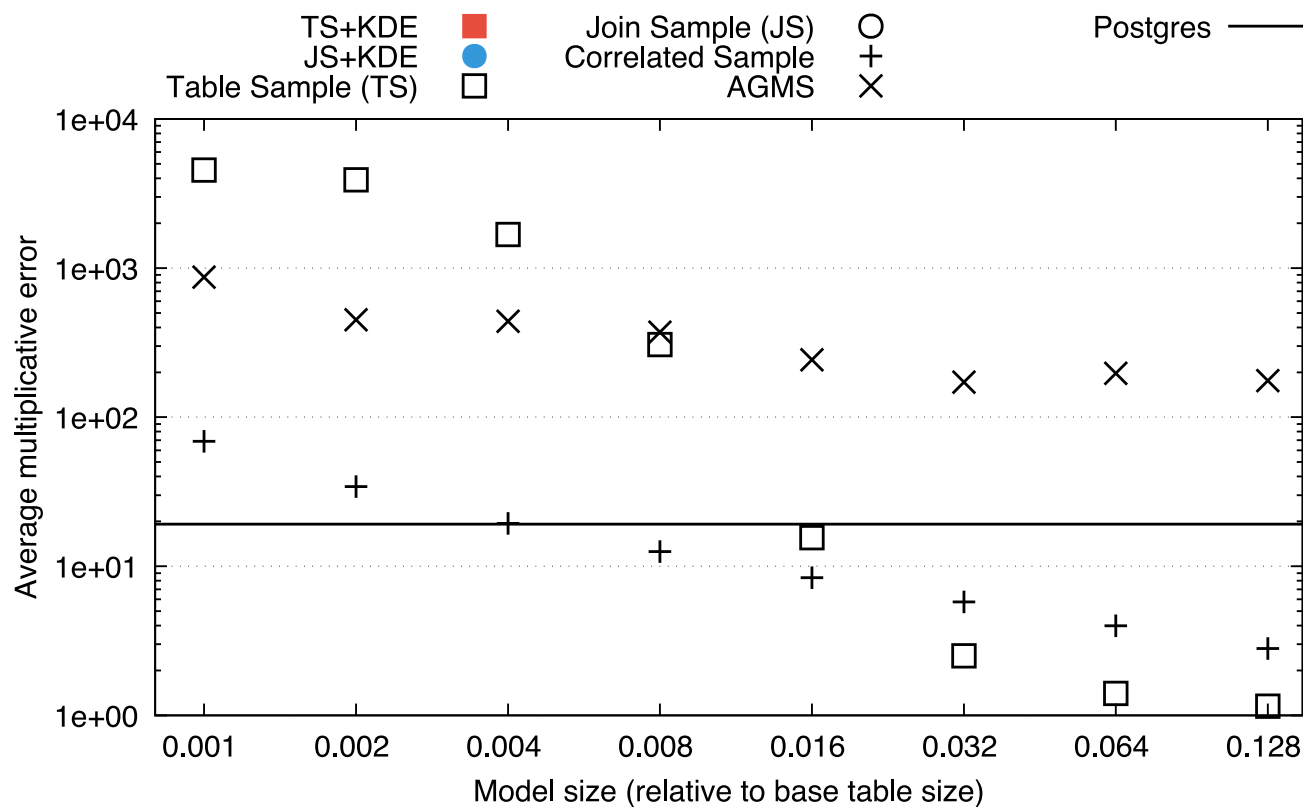
Evaluation: Scaling the Model Size (Correlated Sample)

Dataset: DMV
Query: Q1U



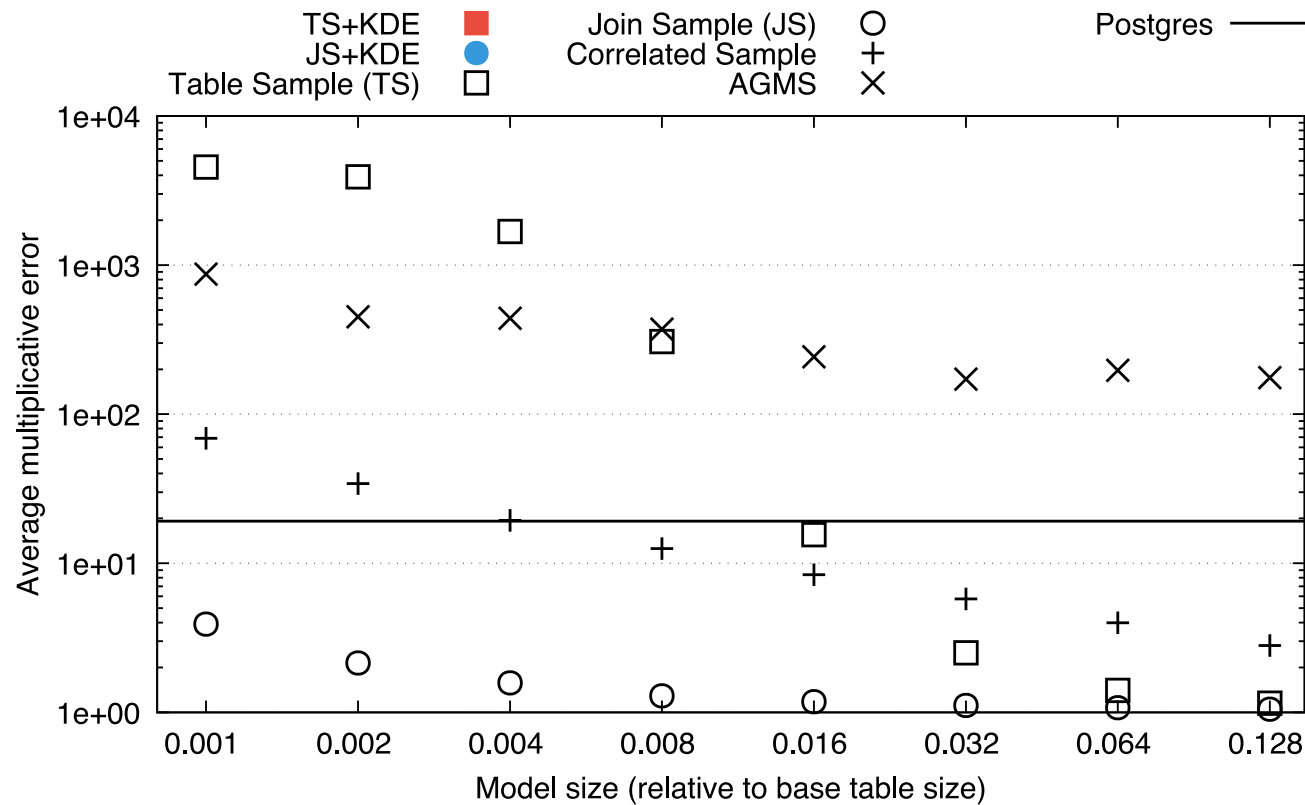
Evaluation: Scaling the Model Size (AGMS Sketch)

Dataset: DMV
Query: Q1U



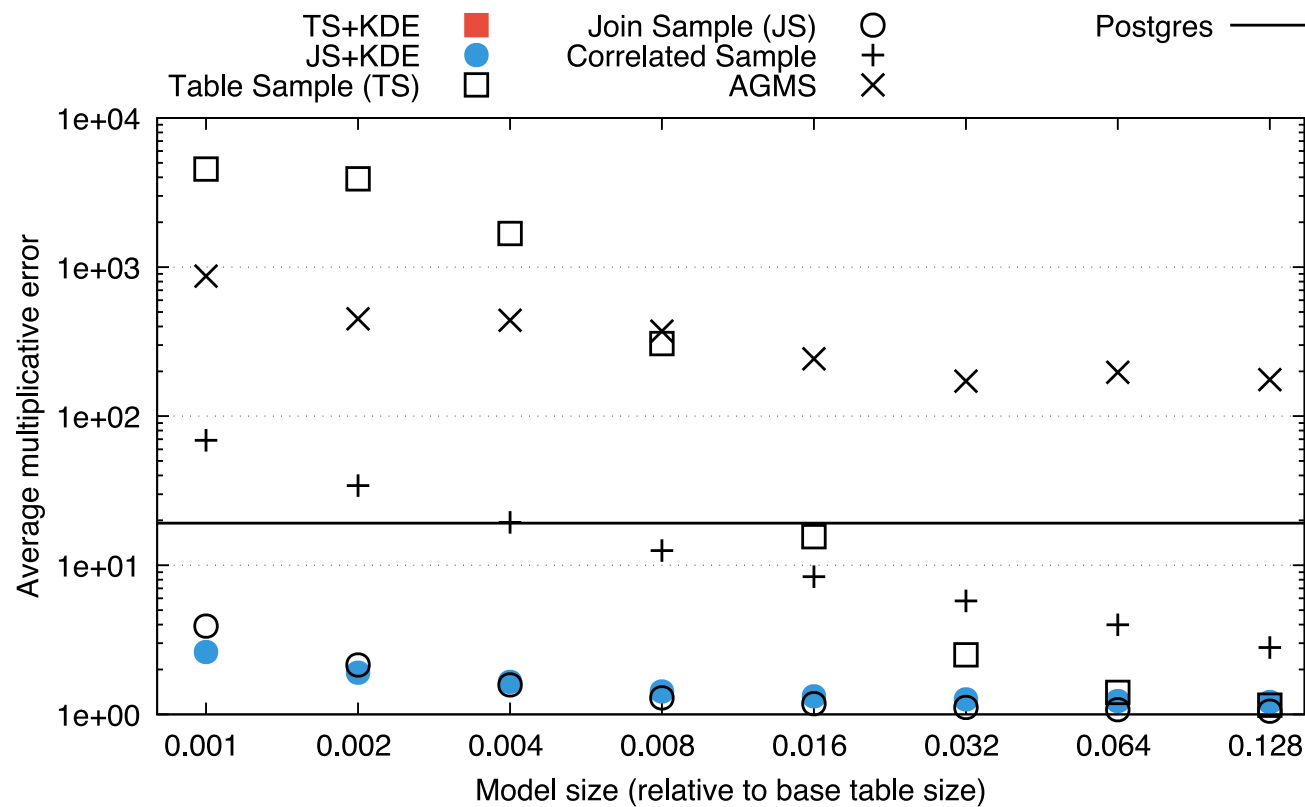
Evaluation: Scaling the Model Size (Join Sample)

Dataset: DMV
Query: Q1U



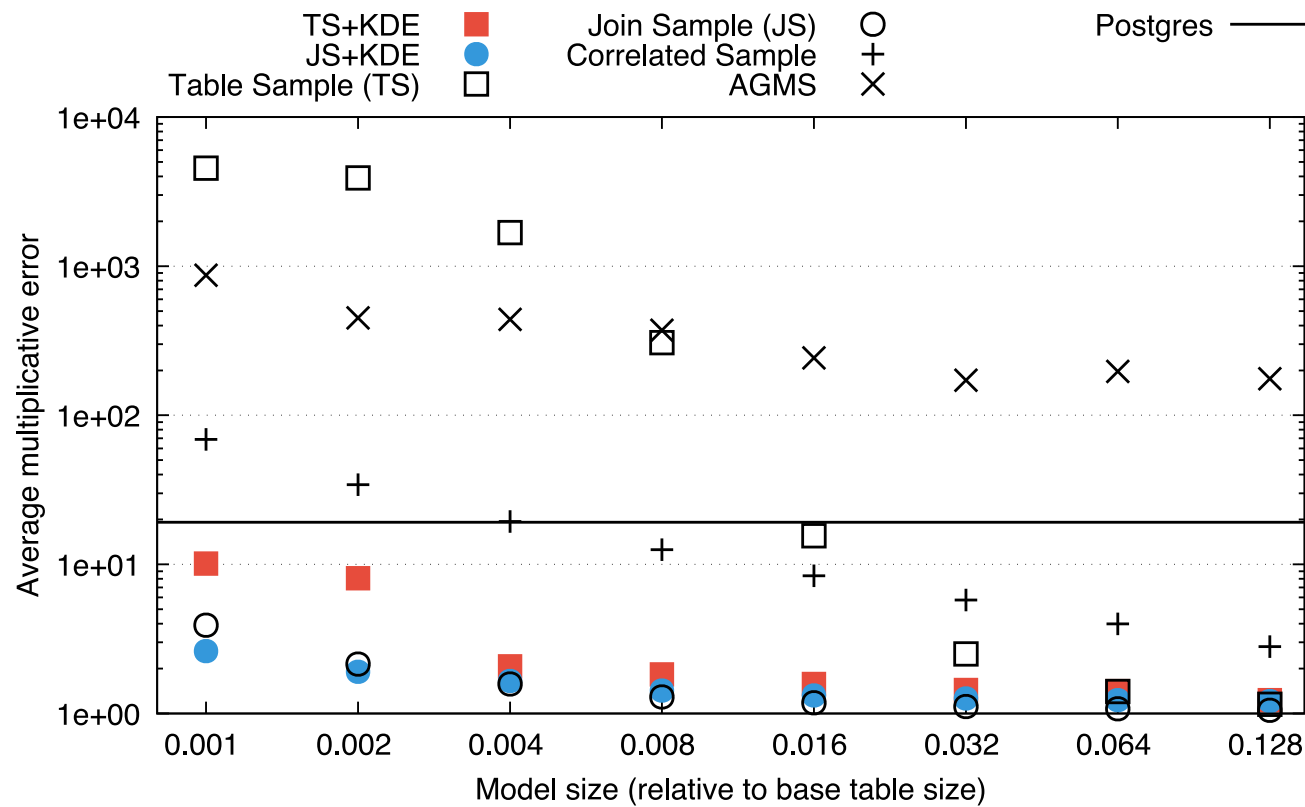
Evaluation: Scaling the Model Size (Join Sample + KDE)

Dataset: DMV
Query: Q1U

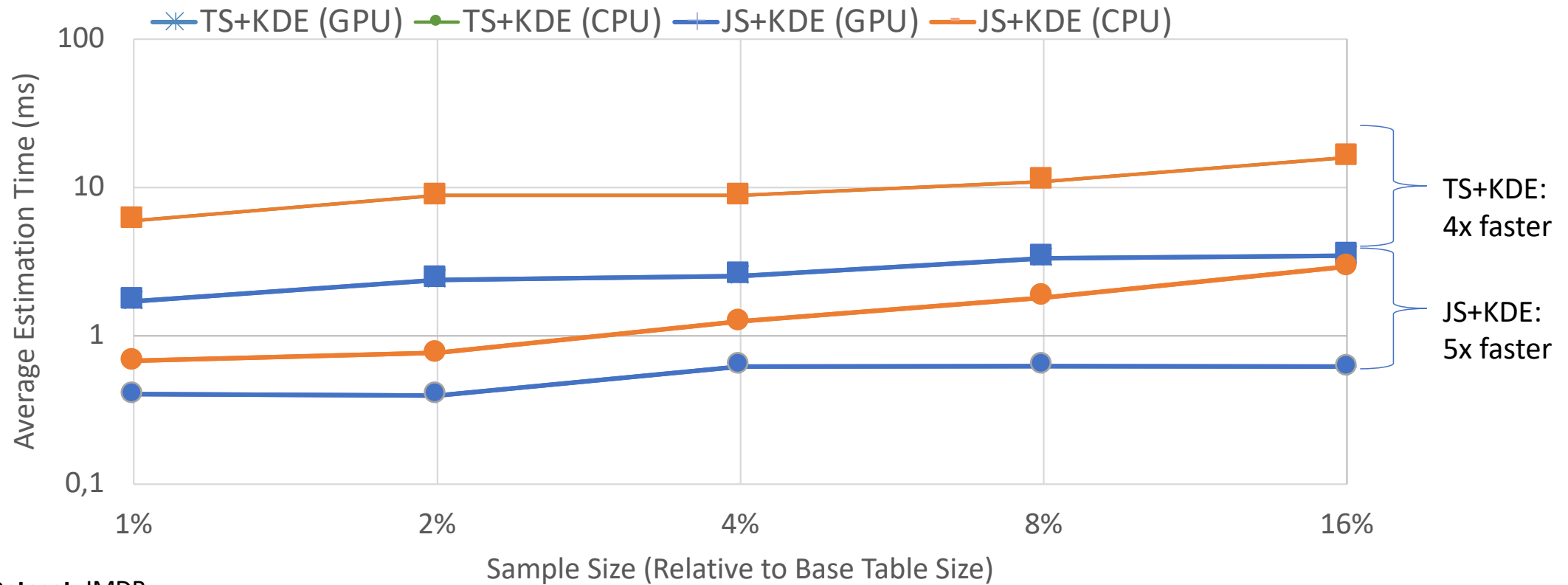


Evaluation: Scaling the Model Size (Table Sample + KDE)

Dataset: DMV
Query: Q1U



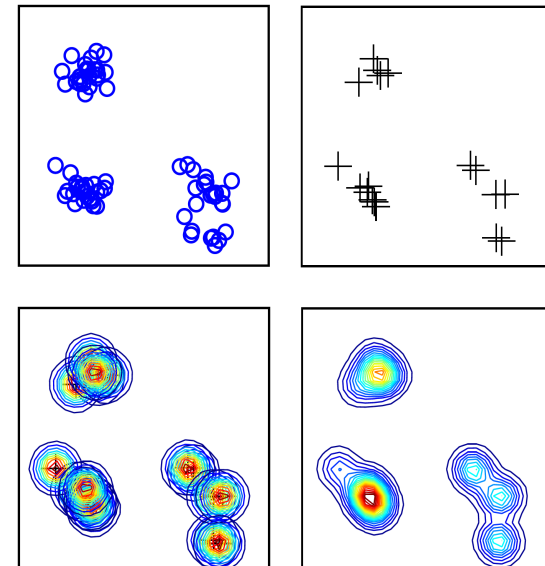
Runtime: CPU vs GPU



Dataset: IMDB
Workload: Q1U
GPU: Tesla V100
CPU: Intel Xeon Gold 5115

Conclusion

- KDE models for join selectivity estimation
- “Getting most out of your sample”
- Based on join or base table KDE models
- Learning hybrid between histograms and samples
- GPU-acceleration possible
- Experiments, data, and code online



github.com/martinkiefer/join-kde

“Estimating Join Selectivities using Bandwidth-Optimized Kernel Density Models”, PVLDB 17

Estimating Join Selectivities using Bandwidth-Optimized Kernel Density Models

Martin Kiefer, Max Heibel, Sebastian Breß, Volker Markl

Proceedings of the VLDB Endowment, 10(13), 2017

Further Publications on GPU-Accelerated Kernel Density Estimation:

Self-Tuning, GPU-Accelerated Kernel
Density Models for Multidimensional
Selectivity Estimation

SIGMOD 2015

Demonstrating Transfer-Efficient
Sample Maintenance on Graphics
Cards

EDBT 2015